

Last class:

eg. An electron and positron annihilate. How much energy is given off?

mass of electron is $9.11 \times 10^{-31} \text{ kg}$ (same for positron).

$$E = mc^2 = 2 \times (9.11 \times 10^{-31} \text{ kg}) \times (3.00 \times 10^8 \text{ m/s})^2$$

$$2 \times 9.11 \times 3 \times 3 = 163.98$$

$$= 1.64 \times 10^{-13} \text{ J}$$

$$2 \times 9.11 \text{ E-31} \times 3 \text{ E8} \times 3 \text{ E8} = 0.0$$

$$\text{or } 1 \text{ MeV} = 1.602 \times 10^{-13} \text{ J}$$

$$\text{the energy released} = 1.6398 / 1.602 = 1.0236$$

$$1.02 \text{ MeV}$$

$$\text{mass of an electron } 9.11 \times 10^{-31} \text{ kg} = 0.511 \text{ MeV}/c^2 = 0.000549 \text{ u}$$

If 1 u of matter is changed into energy, how much is produced in MeV?

u is the atomic mass unit = 1/12 of the carbon-12 isotopic mass

$$1 \text{ u} = 1.66053904 \times 10^{-27} \text{ kg}$$

$$E = mc^2 = 1.66053904 \times 10^{-27} \text{ kg} (2.99792 \times 10^8 \text{ m/s})^2$$

$$= 1.66053904 \times 2.99792 \times 2.99792 = 14.92413502$$

$$\text{exponents: } -27 + 8 + 8 = -11$$

$$14.924 \times 10^{-11} \text{J} = 1.4924 \times 10^{-10} \text{J}$$

$$1 \text{MeV} = 1.60218 \times 10^{-13} \text{J}$$

$$1.4924 \times 10^{-10} \text{J} / 1.60218 \times 10^{-13} \text{J}$$

$$1.4924 / 1.60218 = 0.93148$$

$$-10 - (-13) = 3$$

$$0.93148 \times 10^3$$

931.48 MeV per u annihilated

Binding Energy

We know that carbon-12 has an atomic mass of 12.000000000000000000u (exactly)

but mass of a proton is 1.007825u
and the mass of a neutron is 1.008665u

Do you notice something?

the masses don't add up.

6 protons have a mass of $6 \times 1.007825 = 6.04695$

6 neutrons have a mass of $6 \times 1.008665 = 6.05199$

total mass $6.04695 + 6.05199 = 12.09894$

but carbon-12 has a mass of exactly 12.

What's the deal?

Nuclear fusion happens in stars where Hydrogen and other small nuclei combine form larger nuclei.

Some of the mass is lost- mass defect.

The lost mass changes into energy.

Binding energy is the difference between mass of the protons and neutrons and the mass of the nucleus converted into energy. It is also the minimum energy required to pull the nucleus apart into protons and neutrons.

mass defect=mass of products - mass of reactants
=mass of isotope - (mass of protons+mass of neutrons)

eg. for Carbon-12

mass defect = $12 - (6.04695 + 6.05199) = -0.09894 \text{ u}$

Binding energy

calculate the hard way $E = mc^2$

or use 931.48MeV per u annihilated factor

Binding energy = mass defect in u x 931.48MeV/u

eg. $0.09894 \times 931.48 = 92.16063 = 92.16 \text{ MeV}$

Atoms with more binding energy/nucleon are more stable

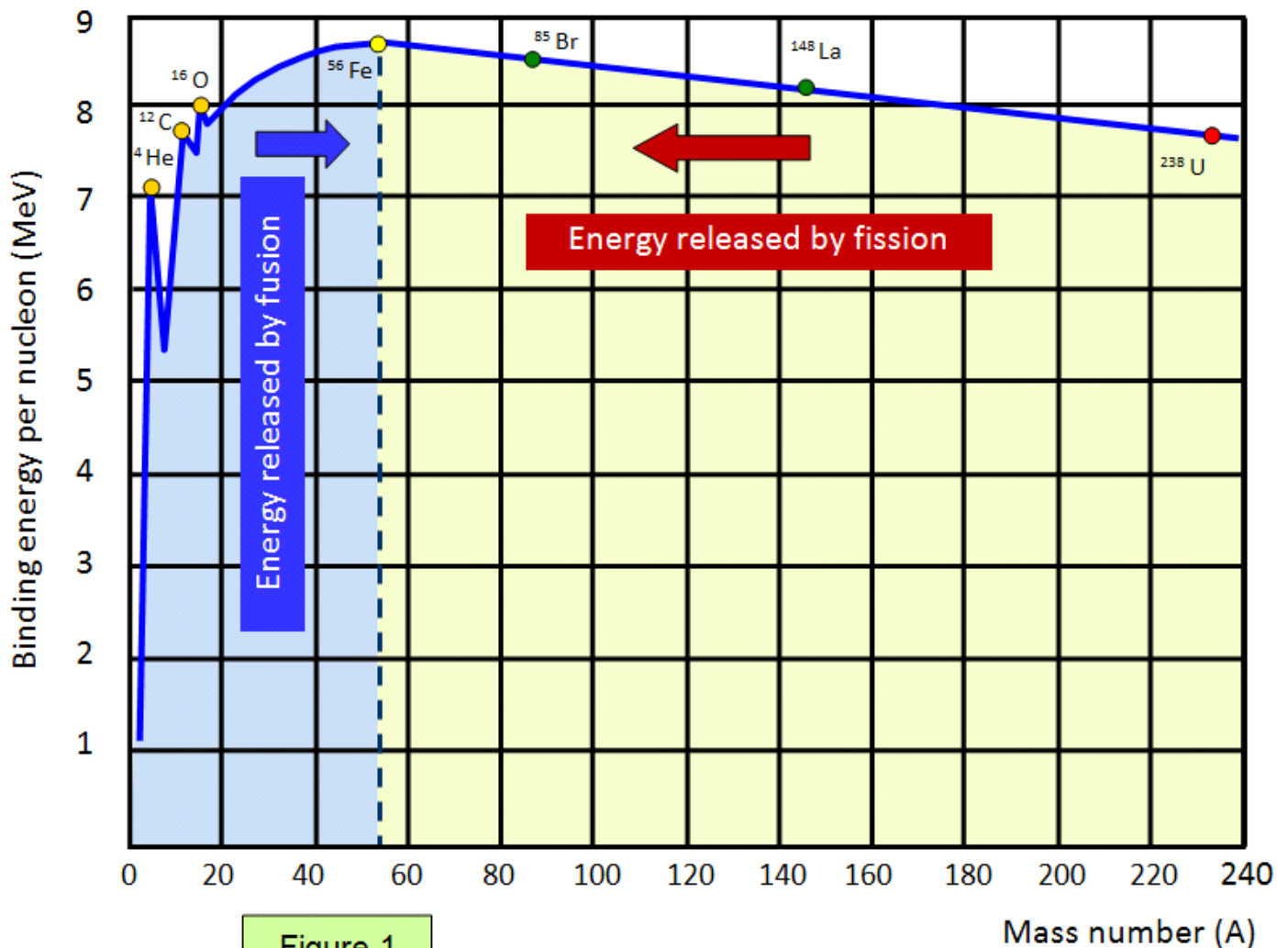


Figure 1

Iron 56 is the highest binding energy per nucleon, so it is very stable. Higher Mass number nuclei are produced in SuperNova or other big energy cosmic events.

Determine the binding energy of Helium 4

isotopic mass = 4.002603u

proton = 1.007825u

neutron = 1.008665u

mass defect = 4.002603 -

$((2 \times 1.007825) + (2 \times 1.008665)) = -0.030377u$

$$((2 \times 1.007825) + (2 \times 1.008665)) - 0.030377 \text{ u}$$

$$\text{binding energy} = 0.030377 \times 931.5 = 28.296176$$
$$28.30 \text{ MeV}$$

p642-645 Q1-8 CR 1.1-1.4
test for March 8th
quiz next Thursday March 2nd